Analysis of Parameters for a Distributed Temperature Sensing based on Raman Scattering

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Abstract—This paper presents a theoretical and computational study on the analysis of parameters for distributed temperature sensing in optical fibers, based on spontaneous Raman scattering effect. The parameters studied were the optical power level, the range of frequency modulation and the length of the sensor element, as well as the application of optical frequency domain reflectometry (OFDR). Two different approaches of reading temperature information from the backscattered signal were also tested. First, one considered the pulse response, and later the ratio between the amplitudes of the detected signals were taken. Such analysis has shown the second method is more efficient to detect the peak of hot spot temperature in the fiber. Spatial resolution equal to 0.96 m and a temperature resolution of 0.089 ºC were achieved using singlemode fiber 30 meters long.

Index Terms — DTS, OFDR, Spontaneous Raman Scattering.

I. INTRODUCTION

Optical fiber sensors have been extensively studied and shown to be very promising for practical applications. Among the reasons one can highlight the commercial potential of this technology, as well as the ability to monitor various physical parameters such as temperature, pressure, strain, vibration, electrical current, and others [1] – [5].

Optical fiber sensing systems base their operation in optical effects, for example diffraction gratings inscribed on the fiber itself [6] – [9], or explore nonlinear optical effects in fiber to measure physical parameters such as temperature, stress and so on [10] – [14]. In the latter type, such nonlinear optical effects are attractive for sensing because they are derived from a natural interaction of light with the medium in which it travels, allowing the fiber itself be the sensing element. It allows a large number of monitoring points [14]. Such characteristics give to this sensing technology based on nonlinear effects an applicability in structural health monitoring of bridges [15], ships [16], dams [14], as well as oil and gas platforms [2].

In this context, the analysis of parameters for optical sensors, is nowadays one of the reasons
involving new research with optical fibers for sensor models showing better results, and to explore new applications [2].

Among the sensors based on nonlinear effects developed, and that meet requirements related to commercial viability, are systems based on spontaneous Raman Scattering (RS) in optical fibers. With applications for distributed temperature sensor (DTS).

The main limitations of DTS systems that can be mentioned are: the low intensity of the received signal, requiring signal amplification [17]; the specific attention during practical operation with the sensor element, which is the fiber itself [3]; determining specific length and adjust of the sensor [17].

In order to overcome such restrictions, research conducted with optical time domain reflectometry (OTDR) explores the use of algorithms applied to the measured data to improve the performance of DTS systems [2], [18].

This paper discusses the main features Raman Scattering in optical fibers for use in DTS systems. It is explored the technique of optical frequency domain reflectometry (OFDR) to optimize spatial resolution and temperature of DTS.

Section II presents theoretical aspects and main equations to describe the spontaneous RS in optical fibers. Section III discusses how to exploit the effect of the spontaneous RS for temperature sensing in fibers. In Section IV is discussed as the choice (or selection) of parameters can affect the performance of DTS systems, bringing also the results of the implementation of the sensor model performed in Matlab®. Finally, the conclusions are presented in Section V.

II. THEORETICAL ASPECTS

High power incident light coupled into an optical fiber will propagate and be spread to effects such as Raman, Brillouin and Rayleigh scattering. If any change occurs in physical parameters, for example temperature, pressure or strain at some point, the change will modulate the signal propagating through the fiber [14]. Thus, by measuring the variation resulting of such modulation, one can perform the sensing along the fiber. This allows obtaining sensors with good accuracy and repeatability in their measures [14]. It is important to emphasize that Raman scattering, Brillouin and Rayleigh occur simultaneously along the fiber, each one depending on a specific threshold of power to be observed.

Therefore, when high intensity light interacts with the molecules that constitute the fiber material, energy exchanges occur between the photons of incident light and the molecules of the material, for instance fused silica. The energy changes generate new electromagnetic fields with different frequencies propagating in all directions within the fiber [14]. If the scattered light has the frequency lower than the incident light, the molecules of the medium will absorb this energy. It means generating scattered photons with lower energy, which is known as Stokes (S) [14].

On the other hand, if the scattered frequency is higher than the frequency of incident light, the
molecules of the medium transfer part of their energy to the photons of incident light. This generates photons with higher energy that is known as Anti-Stokes (AS) scattering [14]. Fig. 1 illustrates the light interaction with the optical fiber with respective mechanisms of scattering observed as a function of the light wavelength, where the peak intensity depends on the temperature (T).

![Fig. 1. Scattering phenomena in fiber [20].](image)

As shown in Fig. 1, the intensity of the Raman upshifted frequency component (Anti-Stokes light) exhibits a strong dependence on the temperature, while the downshifted frequency component (Stokes light) is slightly temperature dependent [19].

The spontaneous scattering is observed when scattered photons are generated independently from other photons; and stimulated scattering, occurs due to photons generated from scattered photons. Raman scattering in fibers spreads in all directions and only a small fraction of this scattering is guided along the fiber [17].

Fig. 2 illustrates the experimental setup to obtain the spectrum of the spontaneous RS. It comprises a pump laser, a fiber optic circulator and the optical fiber where the light propagates. The detector capture the backscattered power spectrum.

![Fig. 2. Setup to measure the spontaneous RS.](image)

The equation that describes the fraction of backscattered power $P_S$ Stokes signal captured and guided along the fiber is [20]:

$$P_S = \overline{P_S} + A_S \cos(\nu_{mod} t + \phi_S) \quad (1)$$

With the average $\overline{P_S}$, the amplitude of Stokes scattering $A_S$, and phase $\phi_S$ defined, respectively, by:

$$\overline{P_S} = P_B n_S \Gamma_S \frac{1}{2\alpha_S} \left[1 - \exp(-2\alpha_S L)\right] \quad (2)$$
\[ A_s = P_B\mu_s\Gamma_s \exp\left(-\alpha_s L\right) \frac{\exp\left(\frac{\alpha_s L\sinh^2\left(\frac{\alpha_s L}{L}\right)}{1 + \left(\frac{\alpha_s L}{L}\right)^2} \right)}{\alpha_s L} \]  
\[ \phi_s = -k_{mod} L - \arctan\left(\frac{k_{mod}}{\alpha_s}\right) + \arctan\left(\frac{\tan(k_{mod} L)}{\tanh(\alpha_s L)}\right) \]

In equations (1)-(4), \( P_B \) refers to the pumping signal modulated with angular frequency \( w_{mod} \) and the group wave number \( k_{mod} = w_{mod} n_{gr} / c \), where \( n_{gr} \) is the group refractive index of the fiber core, and \( c \) the speed of light in vacuum. \( \Gamma_s \) is the Raman Stokes capture coefficient, \( \alpha_s \) the fiber attenuation coefficient for Stokes signal, and \( L \) is the total fiber length.

The Bose-Einstein probability distribution of phonons is written as [21]:

\[ n_s = \frac{1}{1 - \exp\left(-\Delta E/kT\right)} \]  

Here \( \Delta E \) is the difference between the molecule energy levels [20]. \( k \) is the Boltzmann’s constant, \( T \) the absolute temperature of the fiber.

For the Anti-Stokes signal, we have:

\[ n_{AS} = \frac{\exp\left(-\Delta E/kT\right)}{1 - \exp\left(-\Delta E/kT\right)} \]

The equations for the Anti-Stokes scattering signal are similar to those presented above for the Stokes signal. However, replacing in (1)-(4) the index \( S \) by \( AS \).

III. DISTRIBUTED TEMPERATURE SENSOR BASED ON SPONTANEOUS RAMAN SCATTERING

The first approach to read the temperature along the fiber, when the spontaneous RS is generated (see Fig.2) calculates the ratio of the real part of the pulse responses given by [20]:

\[ T(z) = \frac{\Delta E}{k \ln\left(\frac{h_s R_{AS} \alpha_{AS} \left(\frac{\lambda_s}{\lambda_{AS}}\right)^4 \exp(\Delta\alpha \cdot z)}{h_{AS} R_S \alpha_s \left(\frac{\lambda_{AS}}{\lambda_s}\right)}\right)} \]

Where \( R_s \) and \( R_{AS} \) are the responsivity of the avalanche photodiode (APD), respectively to Stokes and Anti-Stokes signals. \( \Delta\alpha \) is the difference between the attenuation of Stokes and Anti-Stokes. \( \lambda_s \) and \( \lambda_{AS} \) are the respective wavelengths for Stokes and Anti-Stokes signals. The term \( h_s \) represents the pulse response of the Stokes signal, given by [20]:
Signals along the fiber to the response for the signal Anti-Stokes is obtained simply replacing the index $S$ by $AS$ in (8). A second approach considered to get the temperature information into the fiber calculates directly the rate $R(T)$ between the Stokes and Anti-Stokes amplitudes given by (3). $R(T)$ is thus defined as

$$R(T) = \frac{A_{AS}}{A_S} = \left( \frac{\lambda_S}{\lambda_{AS}} \right)^4 \exp\left( -\frac{hc'v}{kT} \right)$$

(9)

where $v'$ and $h$ are the wave number separation from the input wavelength and the Planck’s constant, respectively.

Therefore, the temperature $T$ along the fiber can also be estimated by the expression [2]:

$$T(z) = \frac{1}{\frac{1}{\theta} - \frac{k}{hc'v} \ln \left( \frac{R(T)}{R(\theta)} \right)}$$

(10)

The temperature profile is given by the ratio of $AS$ and $S$ signals along the fiber measured in a region where the temperature unknown $R(T)$, and to another region where the temperature is well known $R(\theta)$.

As Stokes and Anti-Stokes waves have different frequencies, they propagate along the fiber with different attenuations. Therefore, to obtain a temperature profile that reproduces properly practical values of the measured temperature, this difference must be taken into consideration [17]. Furthermore, a factor $C$ should be included in the analysis of (7) and (10) to define the constant calibration of the sensor. The value of $C$ depends on the operation conditions of the DTS instrument [10]. This constant allows adjust the modeling with practical issues, such as including losses arising from possible amendments, insertion of further optical components, or disturbances that interfere with the measurement of temperature [10]. The factor $C$ may be thus defined:

$$C = T_a - T_m$$

(11)

where $T_a$ is the actual temperature in the fiber, and $T_m$ is the measured temperature. The calibration should be done assuring the entire fiber length is at the same and constant temperature.

However, to ensure accuracy in the temperature measurement, calibration is not enough. A very
important parameter is the spatial resolution, that defines the spacing between distinguishable adjacent measurement points that ensure accuracy in measurements. In other words, if temperature variations occur in lengths less than the spatial resolution, there is no guarantee the measured temperature obtained is the actual one. The spatial resolution is thus defined [20]:

\[
\Delta z = \frac{c}{2n_{gr} f_{\text{mod, max}}}
\]  

(12)

Where \( f_{\text{mod, max}} \) is the maximum modulation frequency the pump signal.

IV. ANALYSIS OF PARAMETERS AND RESULTS

Fig. 3 shows the diagram based on [2] and [20], which allows discussing the parameters’ analysis performed by simulations for temperature sensing using spontaneous RS.

![Diagram of the possible steps to analyze the output of the DTS.](image)

The diagram in Fig. 3 illustrates three different possibilities to analyze the output of the DTS. The input configuration depends on basically the sensor range intended. For long distances (up to tenth of km), it is preferable to the use of pulsed lasers and the analysis is performed in the optical time domain reflectometry (OTDR). However, for short distances (few km) CW lasers are usually employed with amplitude modulation. Such a configuration is analyzed in the optical frequency domain reflectometry (OFDR).
After defining the analysis domain in the output of the system the next step is the definition of what type of processing to the backscattered power provides better temperature profile. The profile can be evaluated by spatial resolution, range of the temperature, and temperature resolution.

The analysis with OFDR presents two possible configurations, as shown in Fig. 3. The one using the electrical spectrum analyzer (ESA) involves more complex processing. In this case, the amplitude and phase of the signals are stored in the ESA to a post-processing using an Inverse Fast Fourier Transform (IFFT). This procedure allows obtaining the pulse response of scattered signals that carries the temperature information along the fiber.

The configuration of OFDR technique to determine the temperature profile in the fiber by calculating the rate between Stokes and Anti-Stokes spontaneous RS signals amplitudes reduces the processing of data.

Next, one discusses specific parameters in the modeling of DTS.

A. Pumping Power Range

It is shown that the spontaneous RS grows linearly with the power of incident light in fiber [17]. With this information, it is possible to define the range of optical power to be used to generate the spontaneous RS and suppress the effect stimulated that degrades the temperature measure [17], [21].

By calculating the pump power range for generating the Anti-Stokes signal with (1), the obtained curve given by the solid line is shown in Fig. 4. The curve in dashed line indicates the linear behavior of Anti-Stokes component as a function of pumping power.

Fig. 4 shows the pumping power range of Anti-Stokes component is linear with pump power. It indicates a value around 100 mW to be coupled to the optical fiber, corresponding to the region where the curves overlap in Fig. 4. As a result, values lower than 100 mW should be launched to the fiber in order to generate just the spontaneous RS. This result is equivalent to those presented in [17], [20].

Besides, singlemode fibers present reduced diameter of the core if compared with multimode fibers, causing the light to stay confined to a small region at the center of the fiber. This high concentration
of power promotes the emergence of stimulated RS that is not desired, since it interferes with the interrogation of the temperature and cannot be filtered from spontaneous RS. Typical values of power for commercial DTS systems are around 50 mW [17].

The input parameters used in the simulations are summarized in Table I.

**Table I. Input Parameters Considered in the Simulations**

<table>
<thead>
<tr>
<th>Description</th>
<th>Value</th>
</tr>
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<tr>
<td>Frequency range ($F_R$)</td>
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</tr>
<tr>
<td>Number of samples ($N_S$)</td>
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</tr>
<tr>
<td>$\Gamma_S$</td>
<td>3.04x10^{-10} m^{-1}</td>
</tr>
<tr>
<td>$\Gamma_{AS}$</td>
<td>4.00x10^{-10} m^{-1}</td>
</tr>
<tr>
<td>$\alpha_S$</td>
<td>0.210 dB/Km</td>
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<tr>
<td>$\alpha_{AS}$</td>
<td>0.225 dB/Km</td>
</tr>
<tr>
<td>$L$</td>
<td>30 m</td>
</tr>
<tr>
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<td>50 meV</td>
</tr>
<tr>
<td>$T$</td>
<td>300 T</td>
</tr>
<tr>
<td>$n_{gr}$</td>
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<tr>
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</tr>
<tr>
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</tr>
<tr>
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</tr>
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</tr>
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</tr>
<tr>
<td>$\lambda_{AS}$</td>
<td>1451 nm</td>
</tr>
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</table>

**B. Exploring Optical Frequency Domain Reflectometry**

In commercial DTS systems that employs the OTDR technique, a pulse with relatively short duration ($\mu$s) is sent along the fiber and the backscattered signal is detected with high temporal resolution. The range of distance for such systems is typically 10 km [14]. The limitation in the range of the sensor is due to the attenuation losses along the fiber and the laser repetition rate of the laser pump. However, features such as the need for short duration pulses with high peak power; bandwidth required in the order of GHz and fast electronics; make the systems sensors based on OTDR expensive and with complicated implementation [14], [17].

An alternative to DTS systems is the OFDR. In this technique, the laser source is amplitude modulated, so that each increment in frequency results in a new value for the amplitude and phase of the backscattered signal [14]. In this case, the pump power to be launched into an optical fiber can be written as [20]:

$$P_B(w_{mod}) = P_0[1 + \cos(w_{mod}t)]$$

(13)

Where $P_0$ is the amplitude of the signal to be modulated, and $w_{mod} = 2\pi f_{mod}$ is the angular
frequency of modulation, defined by the increased frequency $f_{\text{mod}}$ that modulates the pumping laser source.

Fig. 5(a) shows that for values of spatial resolution lower than 1 m, it is necessary to work with modulation frequencies in the range of hundreds of MHz. However, at high frequencies the backscattered signal presents strong attenuation as shown in Fig. 5(b).

![Fig. 5. (a) Spatial resolution against maximum modulation frequency for the analysis of spatial resolution for OFDR. (b) Frequency response for 4.7 km of fiber.](image-url)

The analysis in the frequency domain shows clearly the frequency component of the backscattered signal where temperature changes occurred in the fiber. Fig. 5 (b) reveals a hot spot in the fiber, observed at a frequency of 0.5 MHz.

The OFDR technology provides an almost invariant spatial resolution along the entire sensor length, which ensures to identify and measure a typical hot spot [23]. This is in contrast to other measurement principles (e.g. laser pulse principle, OTDR), which are sensitive to dispersion effects and therefore affected by a broadened spatial resolution at longer measurement distances; in other words, the hot spot sensitivity of pulse type measurements degrades as a function of distance [23].

C. Fiber Optic for DTS

The intensity of the scattered signal measured at the photodiode is highly dependent on the type of fiber used. Basic parameters in the selection of fiber are the attenuation and the numerical aperture (NA).

A fiber specification such as a high NA means a higher coefficient of capture the scattered signal and enhance the backscattered signal. Therefore, the intensity of backscattered signal is larger for multimode fibers due to present higher NA. However, the attenuation of light propagating in such fibers is higher and spontaneous RS suffers greater attenuation to propagate over long distances, i.e. up to 12 km to DTS. Fig. 6 shows the backscattered power against fiber length that enables comparing the amplitude of backscattered signal in multimode and singlemode fibers in terms of these two parameters.
Fig. 6. Backscattered signal power as a function of fiber length for multimode and singlemode fibers, where Anti-Stokes (centered at 1451 nm) and Stokes (centered at 1663 nm) signals are indicated by arrows.

Fig. 6 shows that the spontaneous RS is detected with greater intensity, for multimode fiber lengths less than 1.5 km, making such fibers proper for sensing in short distances. The analysis also presents that due to low attenuation (in the order of 0.2 dB/km) in the wavelength of 1550 nm, the singlemode fiber best suited to generate the spontaneous RS. Since the scattered signals from this effect have low intensity, singlemode fiber becomes the best choice for sensing long distances due to its low attenuation [17]. Therefore, this fiber is adopted in the simulations carried out in this study.

D. Estimating Temperature

The temperature information along the fiber is contained in the AS signal, as already mentioned. The accuracy in the estimation of the temperature will rely on the signal processing applied (or interrogation technique) to extract the temperature from the values of AS and S signals. Fig. 7 shows the results of temperature estimation through (7) and (10).

Fig. 7. Temperature profile against fiber length showing the hot spot. Simulated 1 obtained with (7) and simulated 2 obtained with (10), compared to a DTS response provided by a commercial DTS model AP Sensing N4385B [1].

The results in Fig. 7 show that calculating the temperature directly determining the rate $R(T)$
among the Stokes and Anti-Stokes signals amplitudes with (10) allows higher accuracy to determine the peak temperature. The characterization curve of the sensor, presented in Fig. 8, can be used to determine $R(T)$.

![Characterization of Stokes and Anti-Stokes amplitudes ratio as a function of temperature obtained by simulation to the modeled sensor.](image)

Fig. 8 Characterization of Stokes and Anti-Stokes amplitudes’ ratio as a function of temperature obtained by simulation to the modeled sensor.

**E. Temperature Resolution**

Another parameter commonly found in DTS systems analysis is the temperature resolution, which can be calculated from the standard deviation of the temperature throughout the fiber. Typically, DTS systems based on Raman scattering present temperature resolution of 0.1 °C [22].

Usually, the temperature resolution is presented as a function of fiber length. Such analysis is shown in Fig. 9 (a). The accuracy of temperature measurements along the fiber is reduced, due to the fact the intensity of backscattered signal measured in the detector is smaller and therefore noisier.

In addition to this already known analysis, we present the error in determining the hot spot as a function of temperature. This information sets an operation limit to the sensor in terms of temperature, as shown in Fig. 9 (b).

![Temperature resolution to 16 km of singlemode fiber. (b) Error in measurement the peak temperature in the hot spot, with $F_R = 1$ KHz to 100 MHz and $T = 27$ °C to 227 °C.](image)

Fig. 9. (a) Temperature resolution to 16 km of singlemode fiber. (b) Error in measurement the peak temperature in the hot spot, with $F_R = 1$ KHz to 100 MHz and $T = 27$ °C to 227 °C.

High temperature measurements could be useful in different scenarios including oil or gas industrial
sectors. The optical fibers are generally protected with a temperature resistant polymer coating (such as polyamide) or some metals such as aluminum or gold for these special applications [24]. However, for real industrial applications, these fibers should be protected from external mechanical actions during installation. In [24] was conducted experiments with temperatures up to 450°C, using OTDR and multimode fibers. The error to determine the temperature was 7.2°C. From the analysis of Fig. 9 (b), errors lower than or equal to 0.5°C, means temperatures below 73°C.

F. Profile of Backscattered Signal

Based on data reported in the literature and in the simulations carried out applying (1), Fig. 10 shows the behavior of the backscattered signal along the optical fiber with temperature varying from 300 to 350°C.

![Fig. 10. Backscattered power as a function of fiber length for different temperatures.](image)

It is possible to confirm the nature of the Stokes and Anti-Stokes signals. It can be observed in Fig. 11 the signals have very low intensity, around –60 dBm or nW. Any incorrect filtering of such signals in the detector, or even small sources of noise can distort the obtained temperature information.

The fiber attenuation of these signals along its propagation is another issue to be addressed in the selection of laser source wavelength in order to coincide with the lowest possible attenuation.

V. CONCLUSIONS

This paper presents the analysis of parameters for distributed temperature sensing in optical fibers, based on spontaneous Raman scattering propagating in optical fibers. The main equations to generate the Stokes and Anti-Stokes scattered signals, which contain the temperature information along the fiber, were implemented and analyzed. The key input parameters were taken from the literature and simulations were performed using Matlab® in order to predict DTS systems and determine the best combination of enhanced parameters.

Two different approaches of extracting temperature information from the backscattered signal were also tested. First, considering the pulse response, and later calculating the ratio the amplitudes of the
detected Stokes and Anti-Stokes scattered signals. Such an analysis has shown that the second method is more efficient to detect the peak temperature in the hot spot in the fiber. It means, it enables a spatial resolution of 0.96 m and a temperature resolution of 0.089 °C for the sensor under study. This performance was obtained to 30 meters of singlemode fiber with pump power equal to 100 mW.

Regarding the range of temperatures evaluated, the error increases exponentially for temperatures around 90 °C. The error is less than 0.5° C to temperatures lower than 73 °C. This indicates the sensor operation limit in terms of temperature. To validate the simulation model, the simulated DTS data is compared to the DTS response provided by a commercial DTS model AP Sensing N4385B.

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