Analysis and Design of a GaAs Monolithic Tunable Polyphase Filter in S/C Bands

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Abstract—This paper proposes a new topology of a 2-Stages Active Polyphase Filter (APPF) in MMIC GaAs technology. This new topology, named “radial”, allows a greater balancing of output signals phases and amplitudes, over the actual APPF’s at the state of the art. In this paper an ex-novo study is shown and synthesis formulas for the APPF are provided. The MMIC simulations in 1-5GHz bandwidth show a tunable Image Rejection Ratio (IRR) greater than 40dB, a worst case input/output matching of 7.8dB and a maximum insertion loss of 10.8dB. By comparison with the tandem topology, as will be shown in the following, the radial one allows a significant improvement in the electrical performances.

Index Terms—Active Polyphase Filter, Tunable Polyphase Filter, monolithic, excitation mode, image reject receiver.

I. INTRODUCTION

Actual mobile telecommunication systems have greatly increased the demand for wideband circuits to transmit and receive a great amount of data while maintaining small dimensions and low cost. Electronic tunability and filtering of the operating frequency is now day a must, and this requirement, together with the need of small dimensions of the system, force many designers to avoid dedicate off-chip filtering sections. In fact, filters, considered as standalone circuits, are quite bulky and costly: for this reason, now day all the filtering is attempted to be realized at chip level.

A common problem in such wideband receivers is to cancel at the greatest extent the image frequency, and one solution to reduce the filtering problem is to employ Image Rejection Mixers (IRM) [1]. Such mixers need quadrature Local Oscillator (LO) signals, and the IRR achievable by such IRM’s is directly dependent by the quality of the quadrature and amplitude unbalancing of these LO signals. So, high quality and wideband quadrature signals generation is a very important requirement in any modern telecommunication systems [2]-[4], and electronic tunability is a great desired possibility.

However, modern telecommunications systems are not the only who need signal quadrature: standard communications systems, as those used by Amateurs Radio, still need good quadrature signals for sideband selection and generation [5],[6].

For all these applications, the polyphase filter [7]-[10], is eventually a valid candidate due its
wideband operation and it is well suited to be simply integrated in MMIC technologies; hence, it is very attractive for a lot of miniaturized and cost effective electronic systems.

Furthermore, it must be considered that the polyphase filter can be used as a phase shifter [11]: by varying the outputs amplitudes, for example using Variable Gain Amplifiers (VGA’s), and combining them it’s possible to change phase of the output signal.

Unfortunately, at the actual state of the art, multistage APPF’s are realized in tandem topology, which are topologically limited by a low balancing of phases and amplitudes of the output signals.

In order to overcome such drawback, in this paper we propose a new PPF topology with synthesis formulas and an useful application example to estimate the powerful of the proposed solution.

This paper is organized as follows:

In Section II the analysis of PPF is briefly exposed, giving expressions for input and output differential impedances. In Section III, the strategy used to select the tuning element is reported. In Section IV, the design of the radial and tandem topologies of the APPF 1-5GHz in GaAs technology is shown. Finally, in Section V we report the conclusions of this work.

II. THE POLYPHASE FILTER SOLUTION

The polyphase filter (PPF) is an n-port electric network composed by a series connection of multiple stages of RC sub-networks, each of them is a ring of resistors and capacitors arranged alternately in a closed loop. In the simplest case, the polyphase filter has 4 inputs and 4 outputs (4I/O), but in the most general case it can have n-inputs and n-outputs. For example, a one stage 4 I/O polyphase filter can be seen in Figure 1: the outputs O₁…O₄ can be considered as 4 unbalanced ones, otherwise as a couple of balanced (or differential) ports O₁-O₃ and O₂-O₄. Between each port and the nearest ones there is a 90° phase difference [1]; for example, the signal taken between the ground and the port O₁ (O₂) and the signal taken between the ground and the port O₂ (O₁) there is a phase shift of 90°. Hence, by taken as reference for instance the signal between the ground and the port O₁, the signals taken between the ground at the ports O₂, O₃ and O₄ have respectively of 90, 180° and 270°: It means that ports O₁ and O₃ and the ports O₂ and O₄ are couples of differential ports and a phase shift of 90° exists between such two couples of differential ports [7]. The main application of the PPF in Figure 1 is that to generate 4 quadrature signals at the outputs, a required function in an image reject receiver or in a SSB modulator for example.

An innovative design approach is proposed in this paper, it is based on a "radial topology", which does not introduce phase and amplitude imbalances. The physical layout can be considered as a design requirement as will be described in this paper. APPF have been implemented in CMOS technology, [12-14] but until now never in GaAs technology. The range 1-5GHz is easily covered in CMOS technology which is inexpensive and the circuit can be included on the same die with other blocks. Good values of IRR are also achieved with more stages. However, in this project, the GaAs technology has been considered because it is a high reliability process with low losses in the
microwave region and a low cost process respect Silicon process especially for relatively small volume production [15-18]. The GaAs APPF proposed in this paper has the same performances in terms of covered bandwidth, insertion loss, matching and IIR, but it has many advantages compared to CMOS APPF mentioned above; it can be developed for working at higher frequencies thanks first to GaAs which has less parasitic capacitances and higher charge carriers drift velocity [19-21]. Furthermore, there are other two advantages that should be considered, GaAs APPF can work in extreme temperature conditions thanks to larger GaAs band gap and it is radiation resistant thanks to absence of gate oxide [22-24], for this reasons it can be used for spatial and military applications.

![Fig.1. One stage, 4-Inputs/Outputs (4I/O) passive Polyphase Filter, loads Z_L are included.](image)

III. ANALYTICAL APPROACH AND DERIVATION OF THE FORMULAS

A. Excitation Mode

There are two ways to excite network in Figure 1: in the first one, named “Type I”, only one half of the inputs are excited, while with second way, named “Type II”, all the 4 inputs are excited. These excitations modes can be seen in Figure 2 and 3.

![Fig.2. “Type I” excitation.](image)

![Fig.3. “Type II” excitation.](image)

With “Type I” excitation, the first and third inputs are connected to the generator, i.e. such inputs have 180° phase difference between them, while with “Type II” excitation the first input with the
second one and the third input with the fourth one are connected together, so that it result in a two input network. The choice of excitation mode determines the characteristics of the differential output signals, as we will show in the following.

B. Transfer Functions

Considering a one stage PPF as those in Figure 1 and that each output is connected to the same load, the two differential output signals are the following expressions (1) and (2):

$$\Delta V_{out} = V_{out1} - V_{out2} = \frac{z_L}{R_1 + z_L + sC_1R_1 z_L} \left( \Delta V_{in} - sC_1 R_1 \Delta V_{ Qin} \right)$$  \hspace{1cm} (1)  

$$\Delta V_{Q out} = V_{Q out1} - V_{Q out2} = \frac{z_L}{R_1 + z_L + sC_1R_1 z_L} \left( \Delta V_{Q in} + sC_1 R_1 \Delta V_{ Qin} \right)$$  \hspace{1cm} (2)  

where $\Delta V_{out}$ and $\Delta V_{Q out}$ are differential output signals while $\Delta V_{in}$ and $\Delta V_{ Qin}$ are differential input signal and $Z_L$ is load impedance of each output. The pole angular frequency of one stage polyphase filter is $\frac{1}{R_1C_1}$. From the above equations we obtain, for “Type I” excitation, the relation

$$\frac{\Delta V_{I out}}{\Delta V_{I out}} = \frac{1}{sC_1 R_1}$$  \hspace{1cm} (3)  

And for “Type II” excitation the relation

$$\frac{\Delta V_{II out}}{\Delta V_{Q out}} = \frac{1 - sC_1 R_1}{1 + sC_1 R_1}$$  \hspace{1cm} (4)  

With simple circuit analysis used above for (1)-(4), it’s possible to calculate transfer functions of multi-stages networks. The previous transfer functions show that with “Type I” excitation the phase difference between the two differential output signal is 90° for all frequencies and load impedances, but they have same amplitude only at each RC pole; instead, while with “Type II” excitation the phase difference between the two differential output signals is 90° only at each RC pole but they have same amplitude for all frequencies and load impedances. Also, network with “Type II” excitation has the insertion loss about 3 dB less than that with “Type I” excitation [1]. The theory exposed above is now applied to a two stage APPF. A two stage type II polyphase filter is depicted in Fig. 4.

![Fig.4. Two stage type II excitation model for polyphase filter.](image-url)
The phase difference between differential ports can be seen in Figures 5 and 6 for both excitation modes; we refer to two stages PPF where poles are indicated by $f_1$ and $f_2$, being $f_1$ the pole of first stage and $f_2$ the pole of second stage, i.e:

$$f_1 = \frac{1}{2\pi C_1 R_1}, \quad f_2 = \frac{1}{2\pi C_2 R_2}$$

(5)

C. Differential Impedances

The overall loss of polyphase filter is composed of two terms: the intrinsic one, and that due to input and output load impedances. Let us indicate with $Z_{S\_diff}$ and $Z_{L\_diff}$ the source and load differential impedance, and with $Z_{in\_diff}$ and $Z_{out\_diff}$ the input and output differential impedances. As an example, for the differential impedances the equivalent circuit at the input can be seen in Figure 7.

![Fig.7. Effect of source termination.](image)

Clearly, in Figure 6 we consider the effect of differential impedance at input; of course, to consider the effect of load termination $Z_{S\_diff}$ and $Z_{in\_diff}$ must be replaced with $Z_{out\_diff}$ and $Z_{L\_diff}$.

Calculating input and output differential impedances for both excitation types, we obtain:

$$Z_{in\_diff\_I} = \frac{2R_1 + Z_{L\_diff} + sC_1 R_1 Z_{L\_diff}}{1 + sC_1 (R_1 + Z_{L\_diff})}$$

(6)

$$Z_{out\_diff\_I} = \frac{2R_1 + Z_{S\_diff} + sC_1 R_1 (R_1 + Z_{S\_diff})}{1 + sC_1 (R_1 + Z_{S\_diff})}$$

(7)

for “Type I” excitation, and

$$Z_{in\_diff\_II} = \frac{1}{2} Z_{in\_diff\_I}$$

(8)
\[
Z_{\text{out, \text{diff}}} = \frac{2R_1 + Z_{S, \text{diff}} + sC_1 R_1 Z_{S, \text{diff}}}{1 + sC_1 (R_1 + 2Z_{S, \text{diff}})}
\] (9)

for “Type II” excitation; these expressions are used for input/output matching.

**D. Image Reject Ratio, IRR**

IRR is the Image Reject Ratio, i.e. it is the ratio between the desired and image signals. IRR depends on the phase and amplitude errors between two differential signals and its relation with them is shown in the following equation derived from Norgaard [5]:

\[
IRR = \frac{1 + 2A_{\text{bal}} \cos(\Delta \theta) + A_{\text{bal}}^2}{1 - 2A_{\text{bal}} \cos(\Delta \theta) + A_{\text{bal}}^2}
\] (10)

where \(\Delta \theta\) is phase error respect \(\frac{\pi}{2}\), while \(A_{\text{bal}}\) is amplitude ratio between two differential signals, i.e:

\[
A_{\text{bal}} = \frac{\text{Mag}(O_1 - O_3)}{\text{Mag}(O_2 - O_4)}
\] (11)

\[
\Delta \theta = 90^\circ - [\text{phase}(O_1 - O_3) - \text{phase}(O_2 - O_4)]
\] (12)

The amplitude ratio \(A_{\text{bal}}\) is obtained by the ratio between the differential output signals’ modulus, the (11) can be write as in (13):

\[
A_{\text{bal}} = \frac{\Delta V_I}{\Delta V_Q}
\] (13)

where \(\Delta V_I\) and \(\Delta V_Q\) are defined in (14) and (15).

\[
\Delta V_I = V_{21} - V_{23}
\] (14)

\[
\Delta V_Q = V_{22} - V_{24}
\] (15)

Defining the IRR parameter in log scale, yields:

\[
IRR_{\text{dB}} = 10 \log(IRR)
\] (16)

The in-frequency behavior of the IRR in dB Magnitude can be shown as in Fig. 8.
An useful information on the character of the proposed circuit can be obtained by observing the behavior of the two parameters from which the IRR depends ($\Delta \theta$ and $A_{bal}$), while changing the frequency of the input signal. As a main feature, there is the complete independence of the amplitude ratio $A_{bal}$ to the frequency of the signal, as shown in Fig. 9. The phase difference $\Delta \theta$ with respect the 90° phase shift between the two signals is an important figure of merit. Such value should be 0° (or 180°) for signals whose phase shift must be 90°; depending on the order into the expression (12). In Fig. 10, the behavior of $\Delta \theta$ is plotted and the operative bandwidth can be observed to have a like constant behavior with a low ripple. The two differential output signals have the same modulus at any frequency but a phase difference between each other of 90° only at the poles’ frequency.

![Figure 9. Amplitude ratio $A_{bal}$ vs frequency.](image)

![Figure 10. Phase difference $\Delta \theta$ with respect the 90° phase shift](image)

The IRR is maximized when two differential signals have 90° phase difference each other and same amplitude, as shown in Figure 11.
Analyzing the expression of the IRR is evident that under ideal conditions, which are $A_{bal} = 1$ and $\Delta \theta = 0$ (or 180°), the IRR tends approaching the infinity.

IV. APPLICATION: GaAs ACTIVE POLYPHASE FILTER

A. Technology

The GaAs technology was used to realize the project of a 2-Stage 4I/O APPF. The technology chosen for the project was GaAs mainly because it is a high reliability and low cost process for relatively small volume production.

The design is based on a numerical simulation of the device with several iterative optimization. Since the simulation has been performed in a factory provided ambient, by employing the library of transistors, microstrips, lumped elements and substrate provided by the foundry, we can consider these result with a nice grade of reliability.

There are two ways to vary the poles in each stage: first, using a FET as a variable transconductance and second, using the FET as a variable capacitance. Our choice was the first and we employed a European Foundry.

Figure 12 shows the transconductance vs. the $V_{GS}$ control voltage (hereinafter named Vtune) for a FET with 30 um gate periphery. The FET was connected in parallel to each resistors of the polyphase network, so that we can vary the poles, and consequently the IRR curve translates inside the request band, simply by varying the $V_{GS}$ voltage.

The JFET channel conducts at $V_{gs}$=0 because it is a depletion device, as the voltage became more negative the channel starts to close and the resistance increases reaching an opened channel at a voltage of -1V.
The FET works into ohmic region where it behaves as a resistor with the following approximated expression (17).

\[ R_{CH} = \rho \frac{L}{tW} \]  \hspace{1cm} (17)

where \( \rho \) is the resistivity of the channel, \( L \) is the length, \( W \) is the width while \( t \) is the thickness of the channel. The transconductance can be approximated by the following expression (18):

\[ G_m = \frac{1}{R_{CH} + R_S + R_D} \]  \hspace{1cm} (18)

In order to compute the transconductance in the factory-provided simulation ambient, the setup shown in Fig. 13 has been implemented. The FET’s transconductance behavior in the bandwidth has been measured through the Agilent ADS software, by employing the vendor’s library model.

### B. Device Design: The Importance of Radial Structure

A schematic of both topologies we have considered, the “modular structure” and the “radial structure”, are given in figures 14 and 15. The principal difference in realizing the physical layout of the “radial structure” is the complete symmetrical disposition of components and transmission lines. This is an important issue in the device performances. By employing the radial design, the device...
compactness can be ensured with the minimum encumbrances as a design requirement, from the beginning of the design. This approach could ensure the needed compactness while ensuring the minimum phase error without phase and amplitude imbalances. The spatial arrangement of components can be evaluated in the first step of the design starting by considering the electrical length of the transmission lines and their impact on the physical lengths.

The design starts with the choice of an excitation type; the “Type II” excitation mode was our choice because it presents a loss about 3 dB less than a “Type I” excitation way. Next step was the choice of a number of stages to cover the entire band 1-5 GHz: two stages were necessary, as shown in Figure 16.
In each stage different poles were chosen to obtain maximum bandwidth. Performing only a circuit analysis it is not evident the effects due to the network’s physical asymmetry, while with RF analysis we understand that the layout of the structure is decisive on the whole electrical performances. To maintain the symmetry of the network a new structure was designed named “RADIAL STRUCTURE”. This structure has two concentric stages as can be seen in the layout of Figure 17. In the left side of the layout, it can be seen the DC power supply line “IN+” and “IN- and the DC input control voltage Vtune, at top and bottom the inputs and left and right the outputs; its dimensions are 1350 um x 1830 um. For comparison, the modular structure layout is shown in Figure 18. It can be seen from Figure 12 that the band of “RADIAL” layout is greater than “MODULAR” one.
C. Simulation Results

Radial and Modular circuits were simulated with Agilent ADS (Advanced Design System) software and the IRR performances have been investigated. By using the theoretical equations given previously, these IRR values correspond to a phase error of about 0.5° and $A_{bal} = 1.01$. As shown in fig. 19, the IRR of the radial structure reaches a value of -45dB at 1GHz for $V_{tune} = -1V$ and it reaches a value of -45dB at 5GHz for $V_{tune} = 0V$, consequently the phase error reaches a value of 0.5°; this value is obtained, varying $V_{tune}$ from 0V to -1V, into the entire range of frequencies 1 - 5 GHz. The insertion losses has also been investigated and the dependence to $V_{tune}$ and frequency is reported in figure 20.

![IRR](image1)

**Fig.19.** IRR for modular layout (red line) and radial layout (blue line) for $V_{tune} = -1V$ and $V_{tune}=0V$.

![Insertion Loss](image2)

**Fig.20.** Insertion loss of a radial structure for both differential outputs $O_1-O_3$ (red line) and $O_2-O_4$ (blue line) for $V_{tune} = -1V$ and $V_{tune}=0V$.

In the following Fig. 21 and 22 the reflection scattering parameter are plotted respectively for control voltage $V_{tune} = -1V$ and $V_{tune} = 0V$, relative to the worst case among all possible $V_{GS}$.

![S11 dB Magnitude](image3)

**Fig.21.** $S_{11}$ dB Magnitude at all ports for control voltage $V_{tune} = -1V$.

![S11 dB Magnitude](image4)

**Fig.22.** $S_{11}$ dB Magnitude at all ports for control voltage $V_{tune} = 0V$.

The phase of both differential signals versus $V_{tune}$ is shown in Fig. 23 and 24, from which is evident that signals have a phase difference of 90° at 1 GHz for $V_{tune} = -1V$ and at 5 GHz for $V_{tune} = 0V$. 

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By analyzing the circuit as formed by lumped elements and considering the frequency range of 1 – 5 GHz we cannot realize that the performance of polyphase filter are also influenced by the symmetry of the network; the radial topology can also be applied at higher frequencies, such as 60/70 GHz for radar applications thanks its symmetry.

At high frequency the different path between the elements (C and R) can change the amplitude and the phase of the output signals leading a differential signals which have no more a difference phase of 90°.

The proposed device offers a global performance increase over the classical poliphase filters [6-13], such as IRR value and matching that can not be obtained in a classical Modular layout configuration.

V. CONCLUSIONS

In this paper, PPF technology has been investigated, in order to respond to the growing demand for very wideband and narrow encumbrance telecommunication devices, such as 4 quadrature signals generators and Phase Shifters, suitable for circuits able to transmit a greater amount of data in line with the new requirements of the modern telecommunication devices. The PPF at the actual state of the art are only the Tandem kind, which are limited by a low balancing of phases and amplitudes of the output signals. We have shown a solution to overcome such drawback, by proposing a new PPF topology with direct synthesis formulas for the device design.

An example of application has been described and compared to the classical solution. The design and performance of a GaAs MMIC 2-Stages 4I/O Tunable APPF working in 1-5GHz bandwidth has been documented. Two types of layout have been proposed, one being the classical tandem connection of stages, and a new one named “radial” which permits a higher symmetry in the signal paths. The performed simulations show that the radial layout for the Tunable APPF has an output signals with a 0.5° phase unbalance, with an 8 dB of worst case matching and a 16 dB of maximum insertion loss. The tunability is obtained by varying the gate voltage of FET’s inside the range 0;-1V, allowing to cover the full 1-5GHz bandwidth.
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