Abstract— In this work, we present a Photorefractive Digital Holographic Microscopy (PRDHM) technique based on the writing-reading holographic process in photorefractive Bi\textsubscript{12}TiO\textsubscript{20} (BTO) crystal using the numerical reconstruction of the phase and amplitude image performed by a Digital Holographic Microscopy (DHM) method. We demonstrate that a holographic reconstructed image by diffraction process in photorefractive BTO crystal can be combined with a second reference beam to form a hologram in CCD plane in a DHM setup. The experimental results in a glass slide resolution target and thin film structure was obtained, where, amplitude, phase and 3D phase images are calculated performing digital reconstruction. This technique presents potentials possibilities to obtain 3D phase image of the microdevices for dynamic holography applications.

Index Terms— holography; microscopy; non-destructive testing; photorefractive materials.

I. INTRODUCTION

Photorefractive holography is increasingly being used for quantitative measurements of the amplitude and phase of the objects waves in static and dynamic process [1-7]. In the photorefractive holography, the holographic recording medium is a photorefractive (PR) material. In PR crystals the holographic grating recording are characterized by following light-induced mechanisms: photorefractive (PR) effect, thermo-optic refractive index modulation or photochromic effect [1]. The PR effect consists on the refractive index modulation through charge carriers photo-induction and linear electro-optic effect; the refractive index modulation by thermo-optic effects is due to temperature gradients on the crystal surface; and the photochromic effect is caused by absorption coefficient modulation for high light intensities. These holographic recording materials present advantages like in situ self-processing of recording medium, indefinite reusability, high resolution and low response time. Moreover, PRCs do not present fatigue in dynamic and reversible processes. Particularly, the photorefractive sillenite crystals, Bi\textsubscript{12}SiO\textsubscript{20} (BSO), Bi\textsubscript{12}TiO\textsubscript{20} (BTO) and Bi\textsubscript{12}GeO\textsubscript{20} (BGO), have been used in holographic interferometry, since many interesting properties qualify them as recording media for real-time holographic interferometry (or dynamic holographic interferometry)
These crystals, in diffusive regimen, present a much faster hologram recording process and provide less noisy holographic images due to their anisotropic diffraction properties, through which the transmitted object wave and diffracted wave present orthogonal polarization since transmitted object wave can be cut-off by polarizer. Usually, in photorefractive holographic interferometry for phase determination is applied the phase-shifting technique [3-6], where the phase of each point (pixel) of the image is calculated using a sequence of intensity interferograms acquired and combined to generate the phase interferogram. Before each interferogram to be captured a known change of phase in the reference beam is introduced. In the phase-shifting techniques, the spatial phase measurements are basically accomplished by changing the holographic interferogram intensity by continuous linear mirror micro-displacements and acquisition of the 3, 4, 5 or more holographic interferograms. Many works contributed to the field of real-time holographic interferometry by phase-shifting techniques with photorefractive crystals [3-6].

In Digital Holography by calculating the complex optical field of an image, the amplitude and phase of the optical field are available for direct manipulation [8-12]. The applications of digital holography to microscopy are particularly advantageous because a single hologram records the information of a three-dimensional object space. These advantages have been noted since early in the development of digital holography and applied to imaging analysis of microstructures and biological microscopy [9-12] using CCD sensor as holographic detector. In off-axis holography the angle of incidence of the reference beam is chosen so that when the hologram is reconstructed, the zero order light may be spatially separated from the diffracted holographic reconstruction. The method of off-axis holography involves a high spatial-frequency fringe pattern that must be sufficiently sampled by the CCD, the spatial resolution of the CCD is an important parameter.

Recently, some works present the combination of the photorefractive crystals and digital holography, since: Zhao et al. [13] used digital holography with Mach-Zehnder interferometer and CCD camera for refraction index change determinations in photorefractive crystals using two holograms (with and without crystal illumination) as usual in holographic interferometry. M. de Angelis et al. [14] studied photorefractive crystals characterization by means of reflection experimental set up for holograms registration based in interferometric techniques. But until now, the photorefractive crystals had not been used as holographic recording medium for digital holographic microscopy with direct phase image reconstruction.

In this work, we present an apparatus in which the combination of the photorefractive Bi\textsubscript{12}TiO\textsubscript{20} (BTO) crystal in diffusion regime as holographic recording medium for writing-reading holographic image and numerical reconstruction by means of a digital holographic microscopy method [15]. We called Photorefractive Digital Holographic Microscopy (PRDHM) and this method allows us to obtain the amplitude and phase images of the micro-structured objects. Additionally, the writing-reading-reconstruction process is an important goal of this technique and it’s a potential system for dynamic holographic microscopy applications.
II. THEORETICAL CONCEPTS

A. Holographic recording process in photorefractive BTO crystal.

In photorefractive holography using photorefractive BTO crystal as the recording medium [1,5], the holographic recording occurs by a refractive index modulation, via photorefractive effect in diffusive regimen and the holographic reconstruction of the object wavefront occur in quasi real-time, where the optical reconstruction of the holographic image is in diffracted wave. If $\lambda$ is the recording wavelength, $\rho$ is the crystal rotator power, $L$ is the crystal thickness, $m$ is the modulation of the incident interference pattern and $2\theta$ is the angle between the interfering beams, the diffraction efficiency of a hologram grating recorded in a PR crystal is given by [2-4]

$$\eta = \left( \frac{\pi \Delta n \sin \rho L}{\lambda \cos \theta \rho L} \right)^2 m^2$$

(1)

The intensity $I_0$ at a point $(x, y)$ resulting from the superposition of the diffracted ($I_{0,D}$) and the transmitted ($I_{0,T}$) intensities is given by [4-6]

$$I_0(x, y) = I_{0,T}(x, y) + I_{0,D}(x, y) \left[1 - e^{-i\tau} \right]$$

(2)

where, $\tau$ is the hologram response (writing or erasure) time. The holographic reconstruction of the object wave, $I_{0,D}(x,y)$, is written as [4-6]

$$I_{0,D}(x, y) = I_{0,R}(x, y)\eta + I_{0,R}(x, y)[1-\eta] + 2g Y \cos \Delta\Phi$$

(3)

where $I_{0,O}(x,y)$ and $I_{0,R}(x,y)$ are object and reference beam intensities, respectively, $g$ is a parameter of the polarization coupling of beams, is the interference term and $\Delta\Phi$ is the phase shift on the object beam.

B. Numerical Reconstruction by Digital Holographic Microscopy

For digital reconstruction, we will use the Double Propagation Method [15] which consists in two steps for wavefront reconstruction, the first propagation until the focal plane [12], Fig. 1(a), later on the complex amplitude of the diffraction pattern in this plane is calculated and it is done a new propagation process until the image plane Fig. 1(b).

This method allows performing the image reconstruction beginning from holograms focused in the CCD plane or out of it and with only one hologram the phase field can be calculated with curvature correction caused by microscopic objective. For the experimental application it is programmed in the reconstruction and processing software [12].
Fig. 1. Double Propagation Method for image reconstruction, where (a) first propagation until the focal plan, and (b) new propagation process until the image plane.

III. EXPERIMENTS

Fig. 2. Experimental Setup for Photorefractive Digital Holographic Microscopy (PRDHM) with photorefractive sillenite Bi12TiO20 (BTO) crystal as recording medium, where M’s are mirrors, BS’s are beam-splitters, SF’s are spatial filter, L’s are lens, Po’s are polarisers, MO is a microscopic objective, PRC is a BTO crystal, SAMPLE is a transparent object and CCD is camera: (a) photorefractive holographic recording process in BTO crystal; and (b) holographic reading for digital holographic reconstruction.

This Figure 2 displays experimental setup for PRDHM. The Fig. 2(a) shows the photorefractive holographic recording process in BTO crystal by diffusive regimen, where, the He-Ne laser beam (\(\lambda = 632.8\text{nm}\)) after passing through a beam-splitter BS1 is divided in reference 1, \(I_{0,R1}(x,y)\), and object, \(I_{0,O}(x,y)\), beams, then these are expanded by SF’s and pass through a lens L’s to correct their parallelism. An objective (50X, 0.95NA) directs the image into the BTO crystal which combines it with the reference beam a 30 degree angle between them and gives the volume hologram recording of the microscopic sample.

The reading-reconstruction process of this technique is displaying in Fig. 2(b), where, the image is...
optically reconstructed by diffraction of reference beam 1, I_{0,D}(x,y), in holographic grating recorded in BTO crystal (equation 3) and these one interfere with reference beam 2, I_{0,R2}(x,y), producing an image hologram

$$I_t(x,y) = I_{0,R2}(x,y) + I_{0,D}(x,y)\left[1 - e^{i\Delta \Psi}\right]^2 + 2\sqrt{I_{0,R2}(x,y)I_{0,D}(x,y)\left[1 - e^{i\Delta \Psi}\right]} \cos \Delta \Psi$$  \hspace{1cm} (4)

where, $\Delta \Psi$ is the phase-shift of the holographic pattern, $I_t(x,y)$, which will be digitalized by CCD camera (ImagingSource Inc) and by digital reconstruction the amplitude and phase image is finally obtained. As it is know a slight angle is introduced between the object and the reference beams in the second interferometer for off-axis holography. The camera uses an array of 1024 × 768 pixels with pixel size of 4.65 μm and 24-bit scale output. An USB-2 cable connects the camera to the computer. The image reconstruction is performed by the HOLODIG program supported in MatLab©[12], using Double Propagation reconstruction algorithms [15].

### IV. RESULTS

For testing the capture system it was used a glass slide resolution target as objet and an objective 50x 0.95, Fig. 3. First, the hologram of the object image is recorded in BTO crystal, in according with Fig. 2(a). In following, the diffracted beam in hologram grating that carried the holographic image (amplitude and phase) and the reference beam 2 produce an image hologram which will be digitalized by CCD camera (this hologram is displayed in Fig. 3(a)). This hologram erasure due the diffracted beam delay. Finally, the images reconstruction (phase and amplitude) was done by mean of the DPM method using one hologram. In Fig. 3(b-c) are displayed the reconstructed amplitude and phase image, respectively, and Fig. 3(d) shows the 3D phase graphic of the number 10 of a glass slide resolution target.

Additionally, we are applying the technique to a thin film in glass plate using objective 50x 0.95. In Fig. 4(a) is displayed the hologram digitalized by CCD camera, Fig. 4(b) the reconstructed amplitude image, Fig. 4(c) the reconstructed phase image, and Fig. 4(d) shows the 3D phase graphic. The results obtained from system are in according with the expected for these objects.
Fig. 3. Results of the glass slide resolution target by PRDHM: (a) reading-reconstruction hologram, (b) intensity image, (c) phase map, (d) phase 3D representation.
Fig. 4. Results of the thin film in glass plate by PRDHM: (a) hologram, (b) intensity image, (c) phase map, (d) phase 3D representation.

V. CONCLUSIONS

In conclusion, we reported on a system for holographic microscopy that uses an integrated system of the photorefractive and digital holography, so-called Photorefractive Digital Holographic Microscopy. The system demonstrates, for the first time (to the best of our knowledge), through a photorefractive holographic recording on a fast photorefractive BTO crystal and reading-reconstruction hologram by digital holographic microscopy method is possible to obtain the amplitude, phase and 3D imaging of the microstructures. The presented results and the uses of photorefractive fast crystals at holographic recording medium indicated this system as potentials for a dynamic holographic microscopy, where using multiplexing device as photorefractive holographic recording process and intensity beams control in reading-reconstruction process possibilities the
recording and reading-reconstruction process can occur in different times.

ACKNOWLEDGMENT

The authors thank financial support from UFABC, CAPES, FAPESP (grant 2009/11429-2) and CNPQ (grant 309911/2011-7).

REFERENCES